# AGE, SIZE AND HOST-PATHOGEN INTERACTIONS

Andy Dobson, SFI Workshop – July 2018 Aging and Disease 1) How does force of infection change with age?

2) Do host-parasite interactions change in hosts with different body sizes?

#### TWO THEMES TO THE TALK

Some patterns, some models, some quite huge patterns and lots of wild speculation!

### AGE IS DIFFERENT FROM TIME....



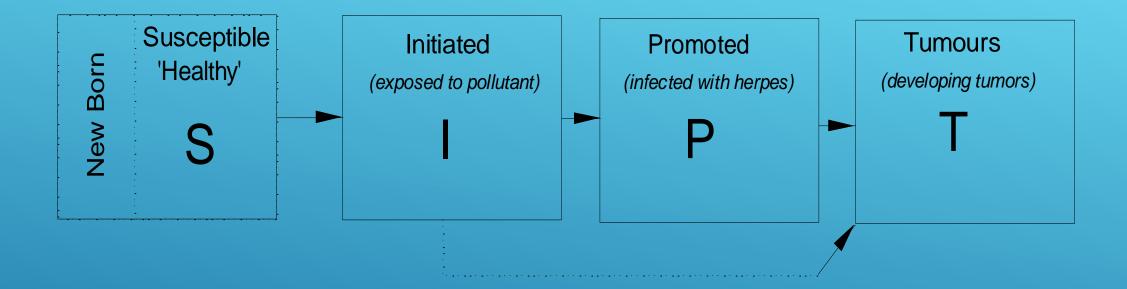
#### 3) GAMMA HERPES IN SEA LIONS STD THAT IS A PRECURSOR FOR VIRULENT TUMORS



JOINT WORK WITH LINDA LOWENSTEIN, FRANCES GULLAND AND BETH BUCKLES, UC DAVIS AND MARINE MAMMAL CENTER, SAUSALITO...AND WITH SARAH COBEY

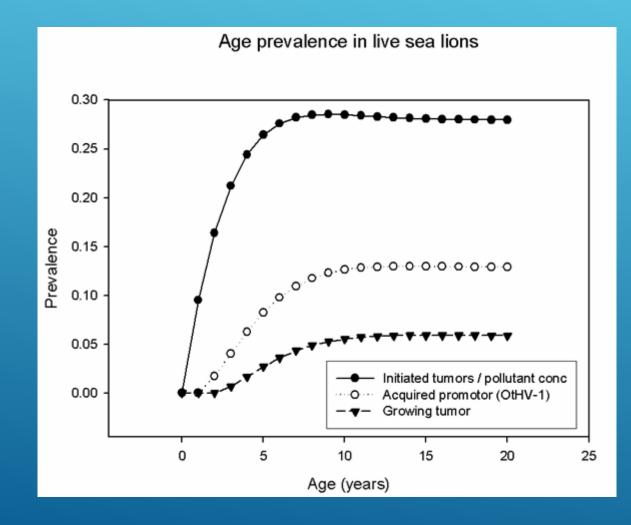
- The models have three major components
- Accumulation and loss of pollutant
  - Mass action through time
- Transmission and impact of pathogen
  - > Frequency dependent, STD model.
- Initiation and promotion of tumor development
  - Modified (dynamic) Doll & Armitage (1954).

# STRUCTURE OF BASIC MODEL

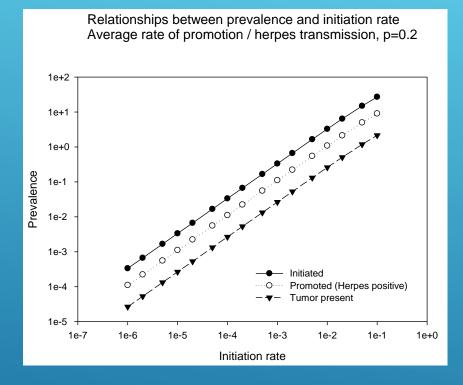


## GAMMA HERPES, DDT AND CANCER IN SEA LIONS

#### GAMMA HERPES & TUMORS IN SEA LIONS

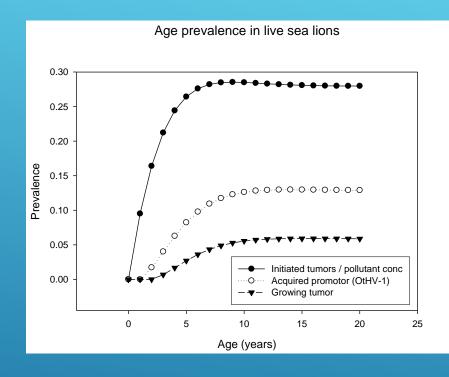


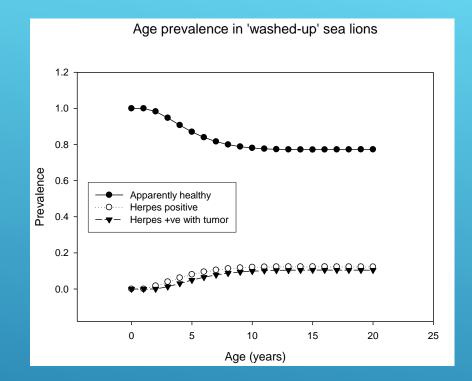




Relationship between prevalence and initiation rate Promotion rate / herpes transmission, p=2.0 1e+2 1e+1 1e+0 Prevalence 1e-1 1e-2 1e-3 Initiated Promoted / herpes positive 1e-4 Developing tumor 1e-5 1e-7 1e-6 1e-5 1e-4 1e-3 1e-2 1e-1 1e+0 Initiation rate

### PREVALENCE AND INITIATION RATE



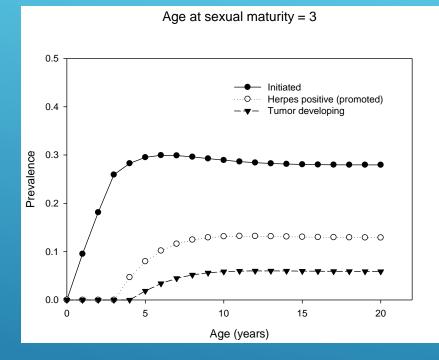


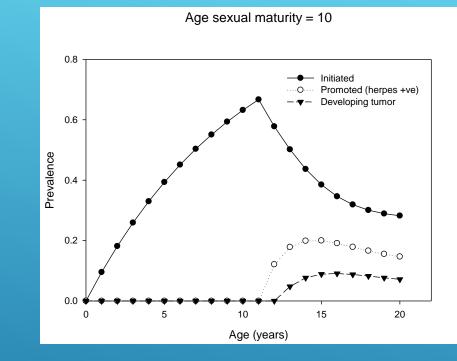
### AGE-PREVALENCE IN BASIC MODEL

The proportion of sea lions with tumors is twice as high in the 'washed ashore' sample than in the 'live' population

#### Females

#### Males



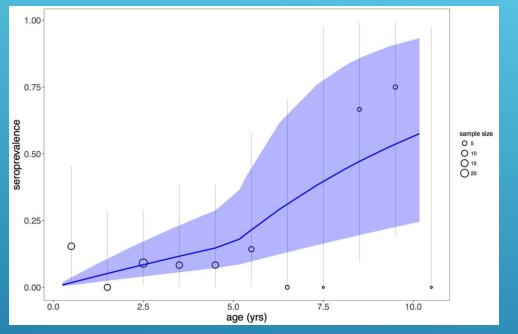


### AGE PREVALENCE & SEX

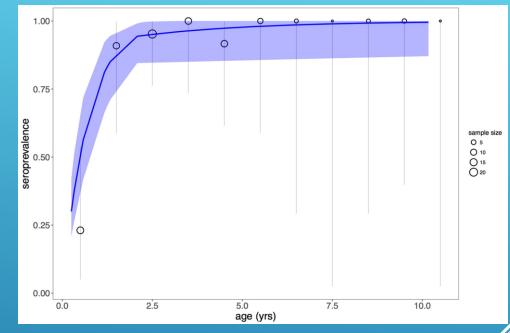
- Data from many human and wildlife diseases can be collected and presented in this fashion
- More characteristic of SIR pathogens
  - Also called a serology profile
- Less common for SEI pathogens
- How do we interpret these patterns?

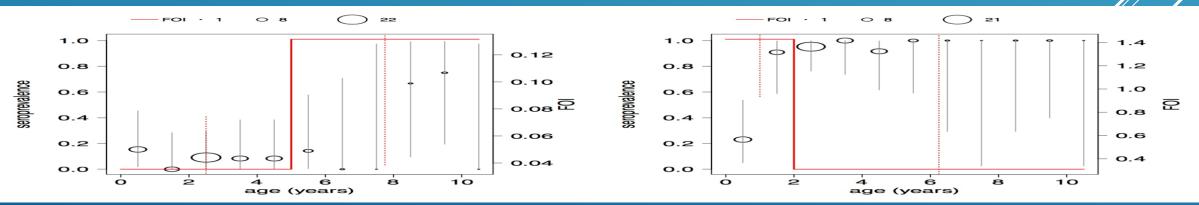
## AGE PREVALENCE CURVES

#### CDV in Minnesota Wolves

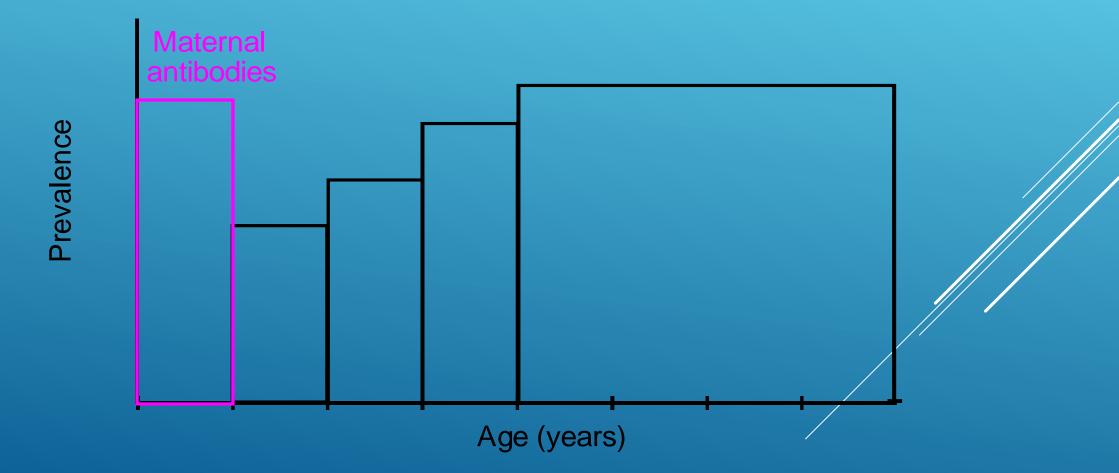


#### CPV in Minnesota Wolves

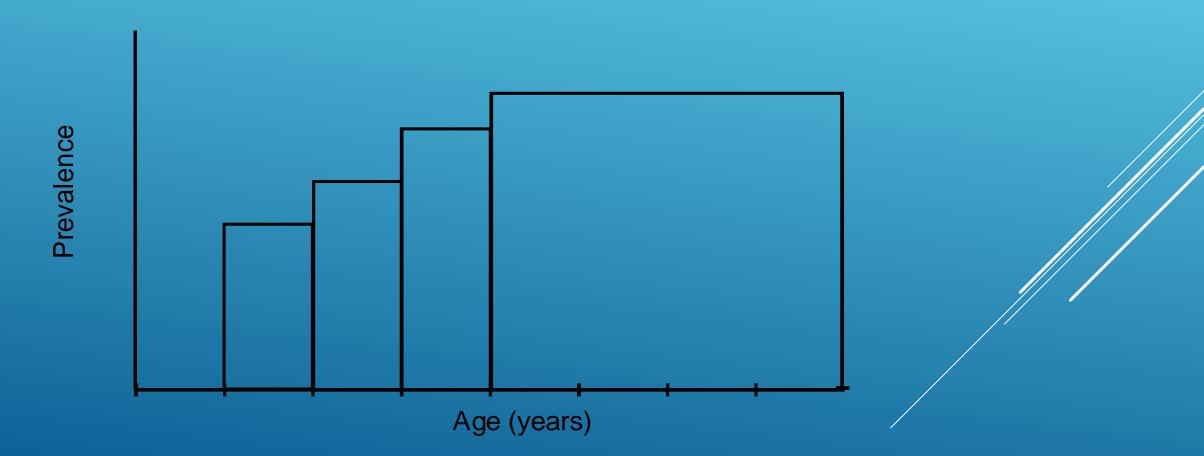


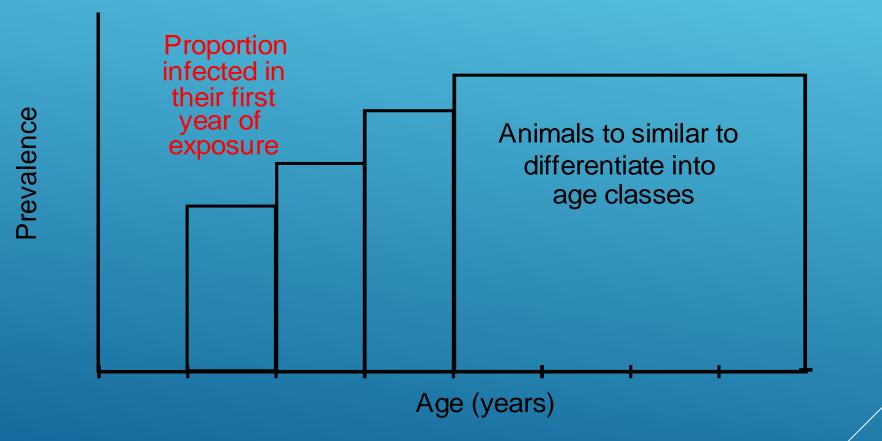


<u>Marie L.J. Gilbertson</u><sup>1</sup>, Ellen Brandell<sup>2</sup>, L. David Mech<sup>3</sup>, Shannon Barber-Meyer<sup>3</sup>, Cara E. Brook<sup>4</sup>, Paul C. Cross<sup>5</sup>, Andrew P. Dobson<sup>6</sup>, Meggan E. Craff<sup>1 (in prep)</sup>



Let's initially ignore maternal antibodies....





So what is force of infection on animals in first age class to be exposed?

Proportion in age class 1 p
Age class 2  $2p-p^2$ Age class 3  $3p-3p^2+p^3$ Age class 4  $4p-6p^2+4p^3-p^4$ Age class 5  $5p-10p^2+10p^3-5p^4+p^5$ 

Note that this begins to form a predictable series..... Pascal's triangle...

- Newly infected in each class.
- > Age class 1
- > Age class 2
- > Age class 3
- Age class 4
- > Age class 5

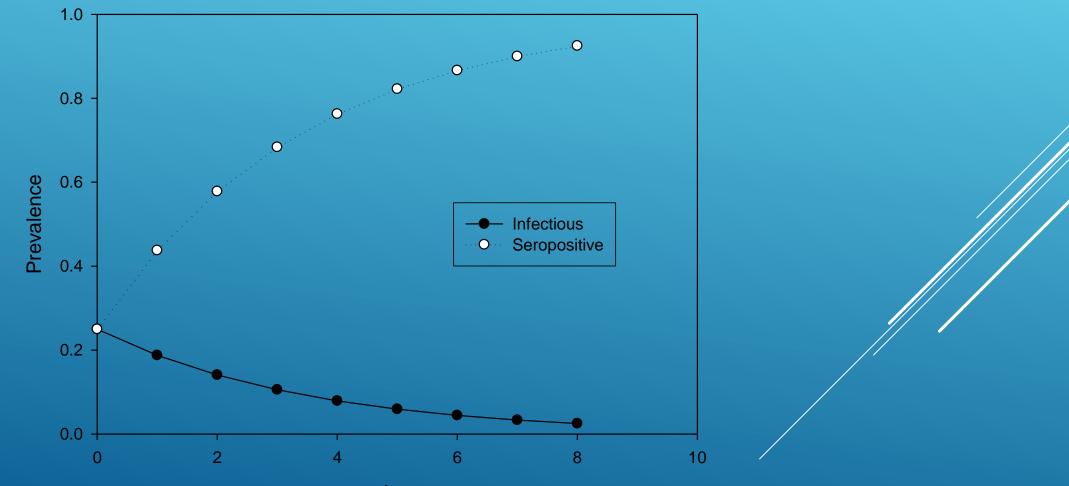
SS.  $p = p^{2}$   $p - 2p^{2} + p^{3}$   $p - 3p^{2} + 3p^{3} - p^{4}$  $p - 4p^{2} + 6p^{3} - 4p^{4} + p^{5}$ 

Note that this corresponds to the relative risk of handling an animal of each age. AND Actual numbers of infected have to have rescaled by ratio of period of infectious to sampling period

Now let's plot these out...

### EXPECTED AGE-PREVALENCE CURVE

Seropositive and infectious hosts



Age

## FORCE OF INFECTION ON ANIMALS IN FIRST AGE CLASS TO BE EXPOSED?

- So what is 'pi'?
- Well if transmission if 'true mass-action', then (in the absence of virulence)
- > Probability of infection

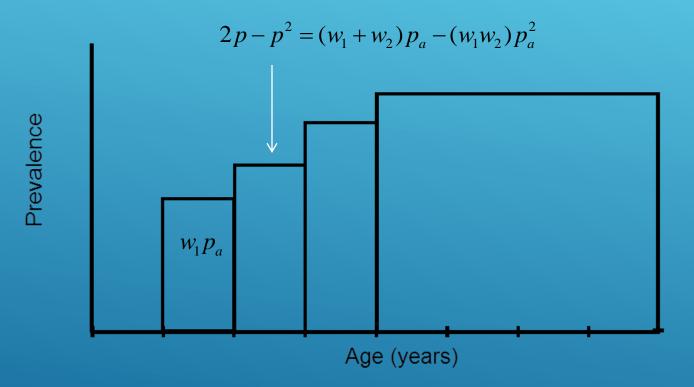
$$p_1 = \frac{\beta I}{N}$$

> Force of infection,

$$\lambda_i = 1 - e^{-p_i}$$

> So if we know age-prevalence, we can estimate Ro?

## WHAT ABOUT DIFFERENCES IN SUSCEPTIBILITY BETWEEN AGE-CLASS?



Assume there is an average probability of infection,  $p_a$  and this is modified in each age class by an age-class specific relative rate of infection,  $w_i$ .

Proportion in age class 1 p
Age class 2  $2p-p^2$ Age class 3  $3p-3p^2+p^3$ Age class 4  $4p-6p^2+4p^3-p^4$ Age class 5  $5p-10p^2+10p^3-5p^4+p^5$ 

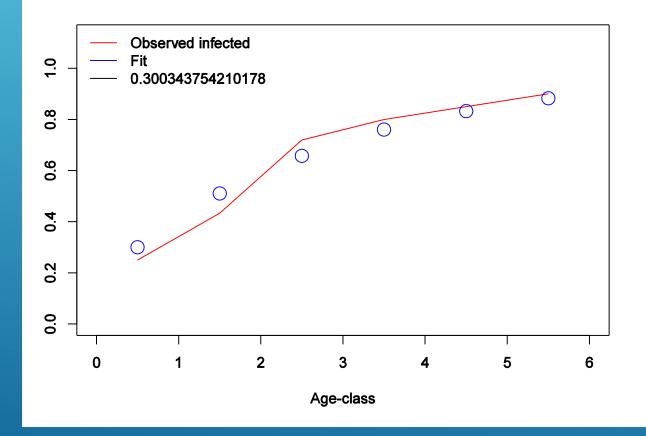
Note that this begins to form a predictable series.....

 $3p - 3p^{2} + p^{3} \Longrightarrow (w_{1} + w_{2} + w_{3})p - (w_{1}w_{2} + w_{2}w_{3} + w_{1}w_{3})p^{2} + w_{1}w_{2}w_{3}p^{3}$ 

Etc...

#### RELATIVELY EASY TO FIT TO AGE-PREVALENCE DATA

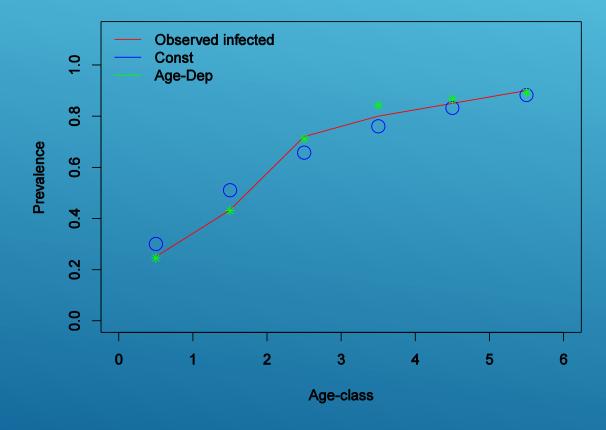
Age-prevalence curve fit with constant "Fol"



Chagas disease in Venezuela, 1960-69.

#### AVERAGE P AND TWO ESTIMATED W'S.

Age-prevalence curve fit with variable "Fol"

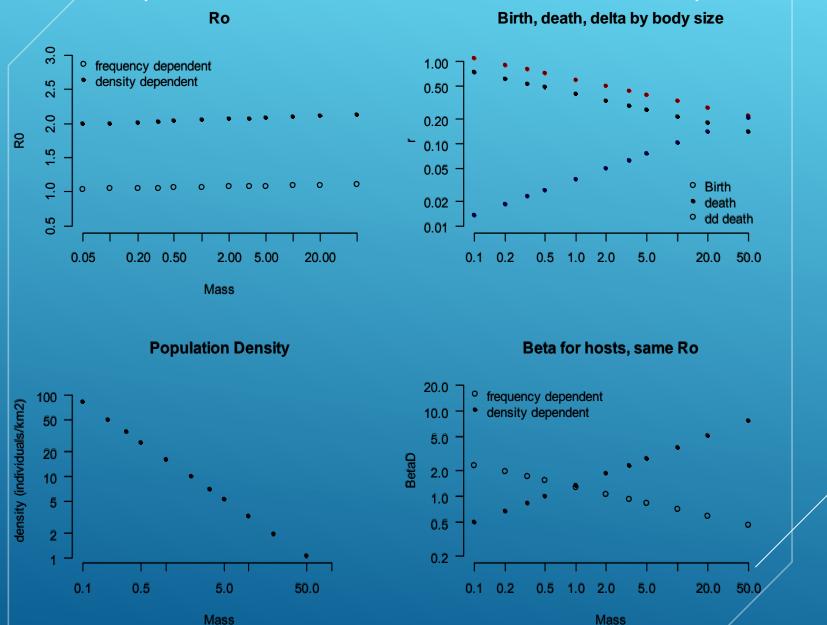


W3,w4,w5>>w1,w2

## BUT WHAT DETERMINES THE AVERAGE RATE OF INFECTION FOR DIFFERENT HOST SPECIES?

All sorts of subtle local climate, habitat, behavioral, genetic differences... Or, one general thing?

#### UNDERLYING DEMOGRAPHY BASED ON ALLOMETRIC SCALING WITH BODY SIZE (DELEO AND DOBSON, NATURE 1997)



# BASIC MULTI-HOST MODEL STRUCTURE.

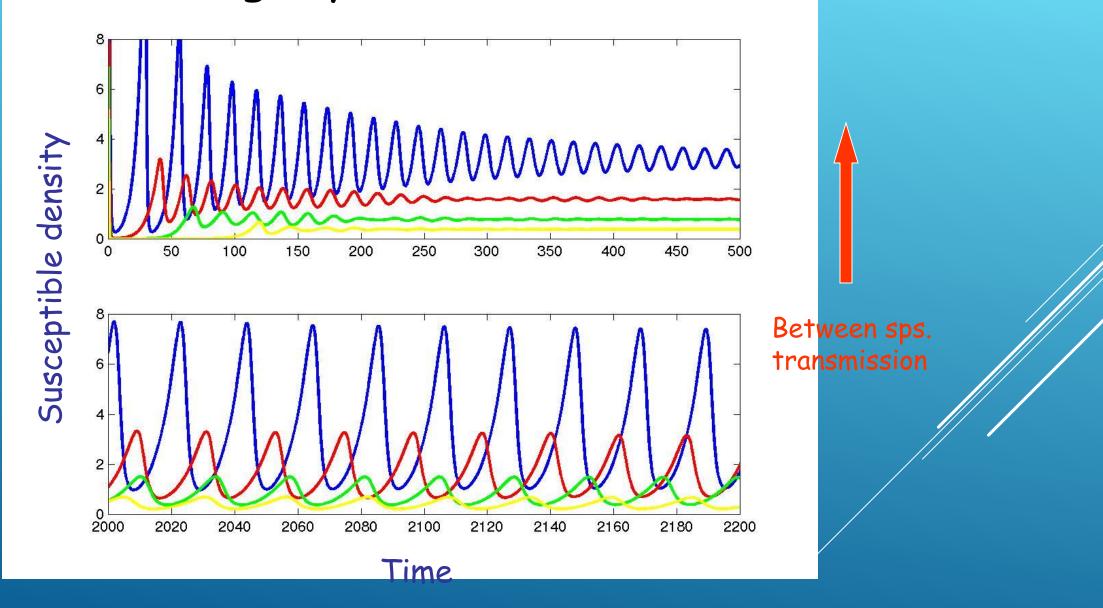
Susceptibles Allometric scaling of all birth and death rates  

$$\frac{dS_i}{dt} = (b_i - d_i - \Delta_i (S_i + I_i))S_i - (\beta_{ii}I_i + \sum_{j \in I_i} \beta_{ij}I_j)S / (\sum_{j=1,n} N_n)^c$$
Within Between  
Infecteds  

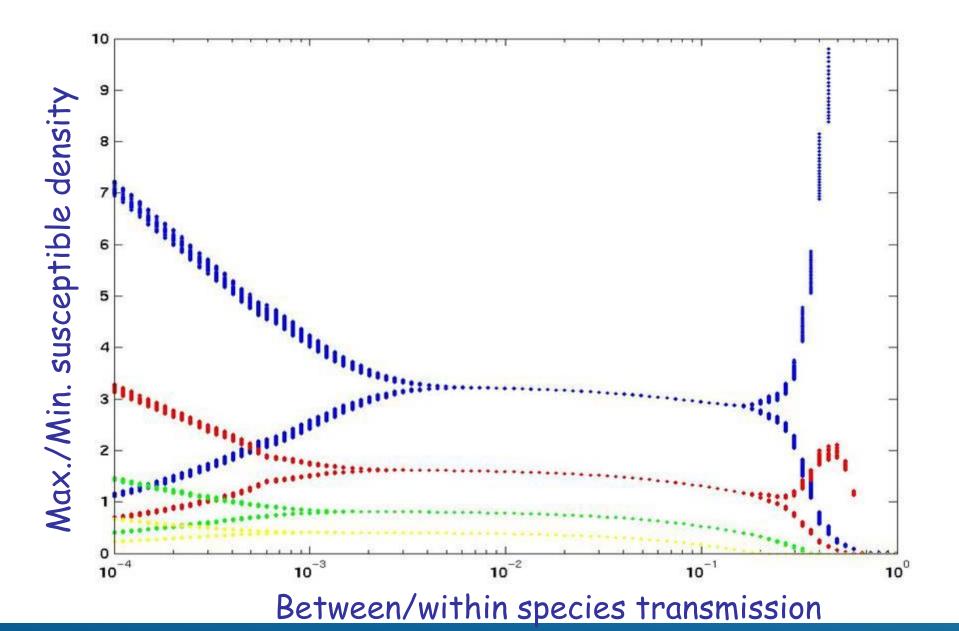
$$\frac{dI_i}{dt} = (\beta_{ii}I_i + \sum_{j \in I_i} \beta_{ij}I_j)S / (\sum_{j=1,n} N_n)^c - d_i(1 + \alpha_i)I_i$$
Scale virulence  
as a proportion  
of life expectancy  

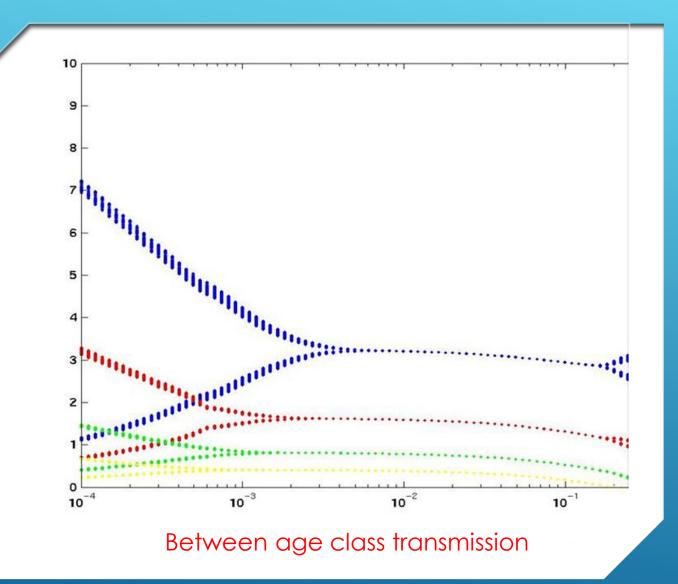
$$\beta_n = c_i \sqrt{\beta_n \beta_n}$$

## Buffering: dynamics in DD case



### BUFFERING: DYNAMICS IN DD CASE





Would we see similar
 effects if Hosts of
 Different AGES
 illustrate different
 durations of
 incubation and
 Infectivity?

#### Prepatent period x size

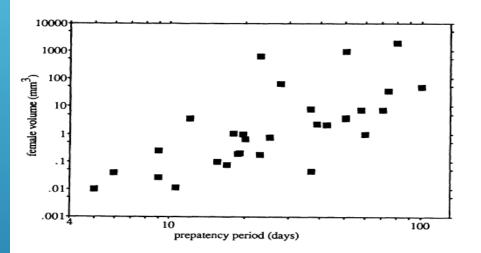


Fig. 1. Log-log plot of the association between prepatency period and female body volume across generic means. r = 0.70,  $\beta = 2.61$ , p < 0.0001, n = 31 genera, based on 49 species.

#### Fecundity x size

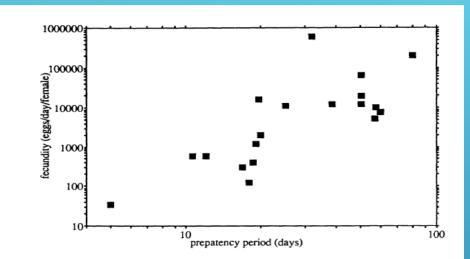


Fig. 2. Log-log plot of the associations between prepatency period and fecundity across generic means. r = 0.77,  $\beta = 2.66$ , p < 0.0001, n = 19 genera, based on 28 species.

## WHAT ABOUT ALLOMETRIC SCALING OF BOTH HOST AND PARASITE?

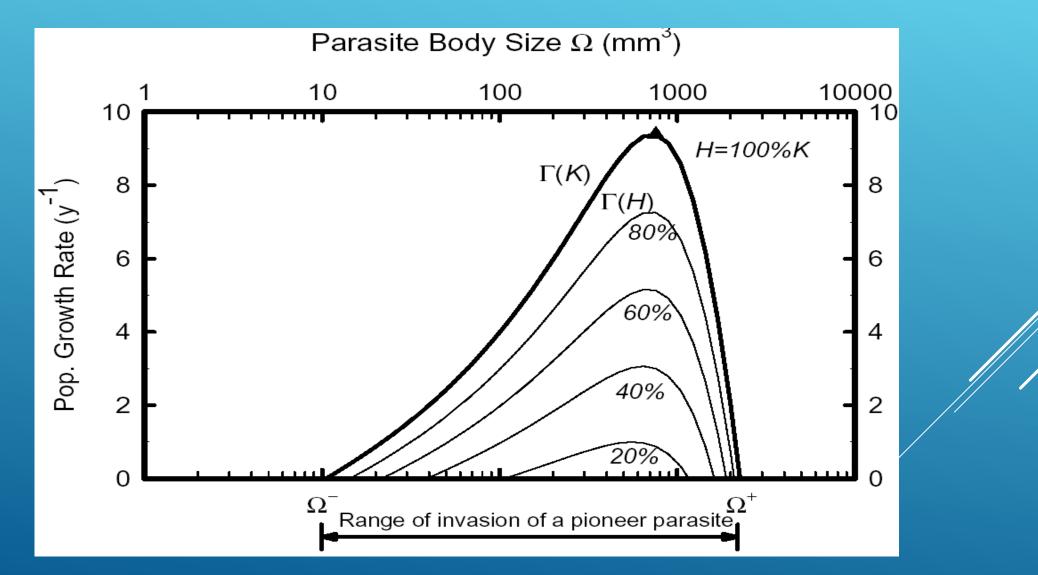
(From Skorping, Read and Keymer, Oikos, 1991)

Host				
	Parameters	Units	Function/value	References
Κ	Parasite-free carrying capacity for mammalian herbivores	No. km <sup>-2</sup>	$=103 W^{-0.93}$	Peters (1983, p. 167)
r B	Per-capita growth rate Per-capita mortality rate		$=0.9 W^{-0.27}$ $=0.4 W^{-0.26}$	Damuth (1981), Peters (1983) Peters (1983), Calder (1984), Schmidt-Nielsen (1984).
			Parasite	
	Parameters	Units	Relationships	References
λ	Per-capita fecundity	Eggs day <sup>-1</sup>	$=10^{3.5} \Omega^{0.79}$ =10 <sup>1.4</sup> $\Omega^{0.24}$	Hechinger et al. (2012)
T	Time to maturity	Days	$=10^{1.4} \Omega^{0.24}$	Hechinger et al. (2012)
Pat	Patent period	Days	$=1.15 \text{ T}^{1.498}=1.15$ $(10^{0.14} \Omega^{0.24})^{1.4.98}=144 \Omega^{0.359}$	RMA regression on Skorping et al.'s (1991) data digitized from Fig. 3
μ	Mortality rate of adult parasites	Day <sup>-1</sup>	$=1/Pat = 0.00693 \Omega^{-0.359}$	
σ	Maturation rate	Day <sup>-1</sup>	$=1/T = 0.0398 \ \Omega^{-0.24}$	
$\boldsymbol{S}$	Fraction of worms surviving to age at maturity		$= \sigma(\Omega) / [\sigma(\Omega) + \mu(\Omega) + \mathbf{b}(\mathbf{W})]$	As in Morand and Poulin (2002)
k	Clumping parameter	A dimensional	Between 0.01 and 1	Shaw et al. (1998)
$H_{\circ}$	Seminaturation constant	No. km <sup>-2</sup>	Set up for any host body size W so that $R_o \leq 10$	
α	Per-capita, per-worm, parasite induced mortality	# of host · # of parasite <sup>-1</sup> · time <sup>-1</sup>	$W \text{ so that } R_{\circ} \leq 10$ $= \varepsilon \ \Omega^{q} / W^{0.75}$	This study. Parameters $q$ and $\varepsilon$ set so that the resulting allometric relationship between host body size (kg) ar parasite body size (mm <sup>3</sup> ) coincides with that estimate empirically by Morand and Poulin (2002).

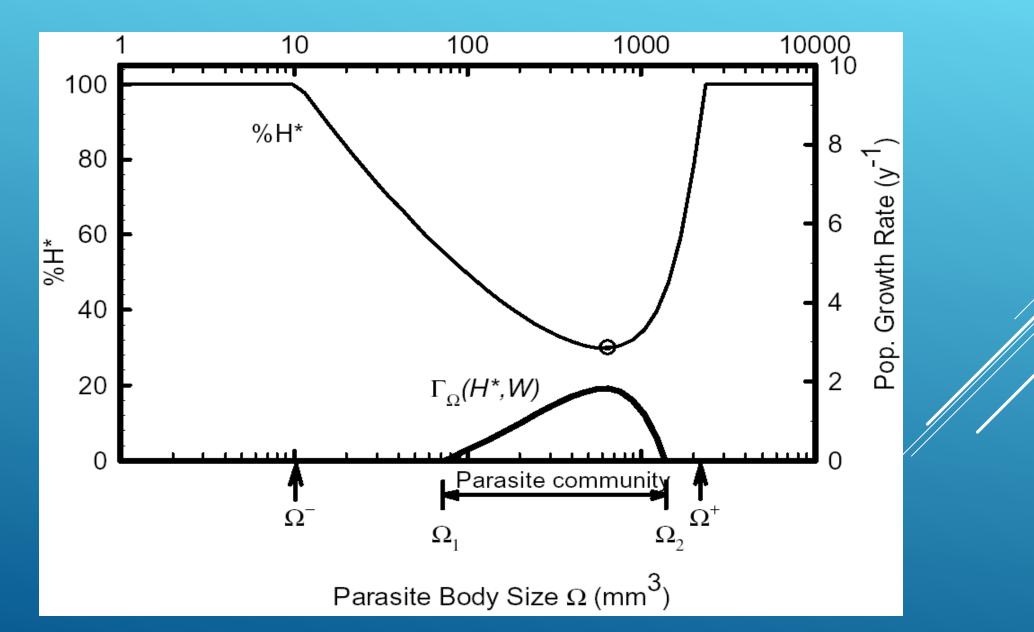
Table 1. Summary of main model parameters and their allometric relationship with body size, along with unit of measure, the corresponding reference and the formula used to compute them. W [kg] is host body size and  $\Omega$  [mm<sup>3</sup>] is parasite body size. Data for prepatent and patent period were extracted from Fig. 3 of Skorping *et al.* (1991) and analysed with Ranged Major Axis Regression on the log-log transformed data with LMO DEL2 in R: slope = 1.498, confidence interval [0.839, 2.405]; intercept = 0.142, confidence interval [-2.706, 2.211]; n = 24, r = 0.666, P < 0.001

#### DeLeo, Gatto and Dobson, Parasitology, 2015

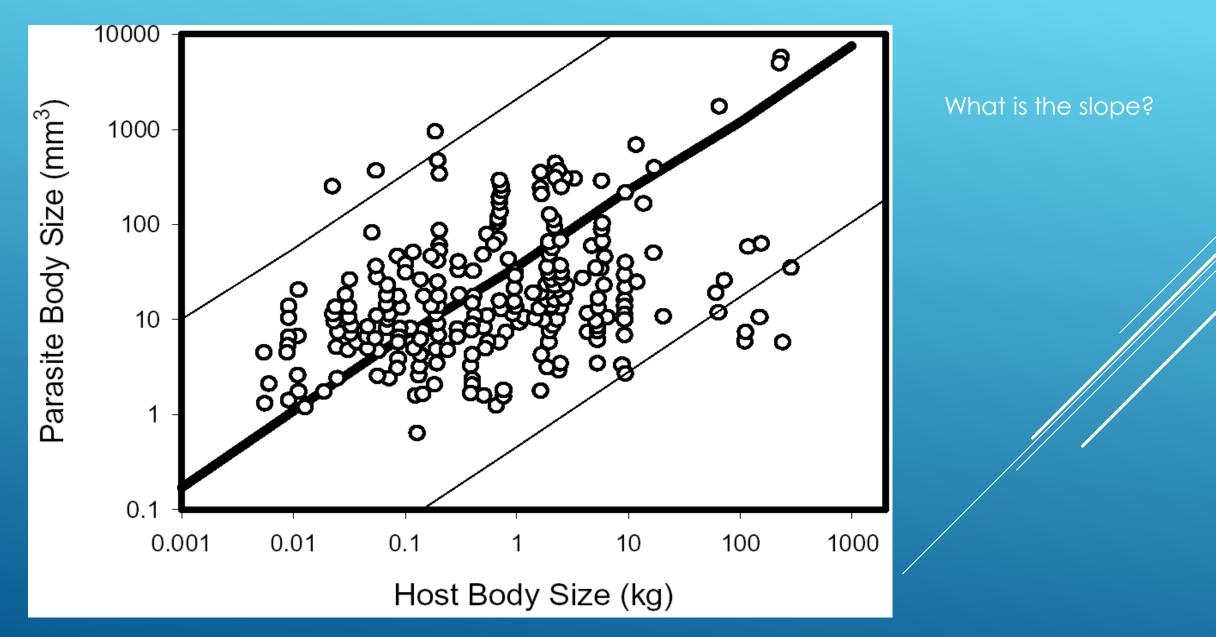
# ALLOMETRIC SCALED DYNAMIC MODELS FOR PARASITIC NEMATODES AND THEIR HOSTS

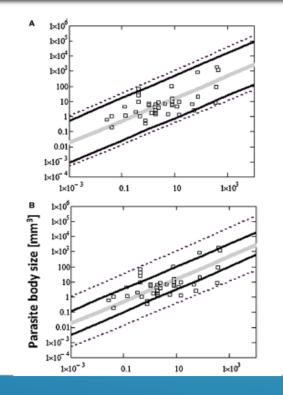


#### INVASION CRITERIA VERSUS EQUILIBRIUM COMMUNITY



### MODEL FIT AND OBSERVED DATA





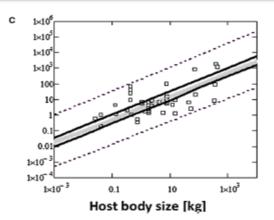
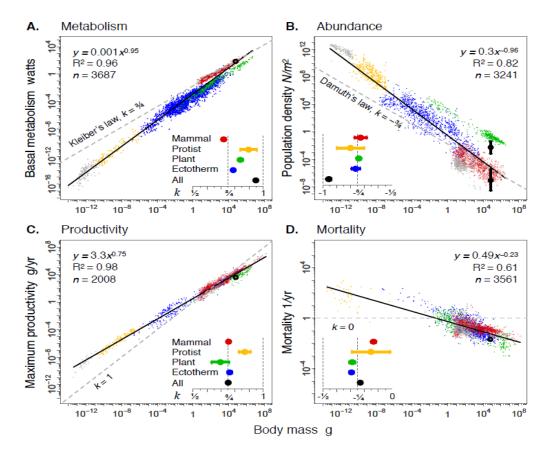
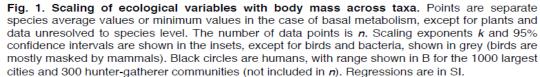


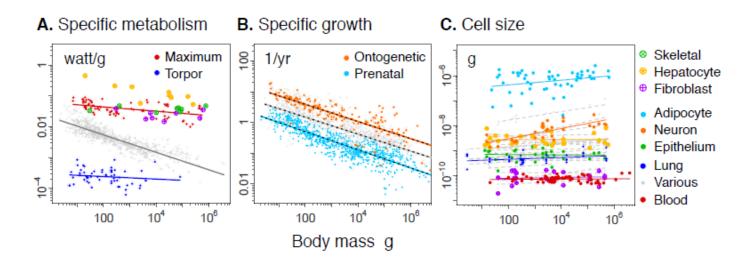
Fig. 2. The relationship between host body size and parasite body size. The open squares represent the data derived from Morand *et al.* (1996). The thick grey line represents the body size of the parasite dominant species for any host body size. The lower and upper dashed lines delimit the range of parasite size  $\Omega^-$  and  $\Omega^+$  able to invade and establish in a population of uninfected hosts at carrying capacity as predicted by our theoretical model. The upper and lower black lines delimit the range of body sizes  $\Omega_1$  and  $\Omega_2$  of parasites that can invade and coexist with the dominant species. (A) Clumping parameter k = 0.01; (B) k = 0.1; (C) k = 1.

RELATIONSHIP BETWEEN HOST BODY SIZE AND NEMATODE PARASITE BODY SIZE (SLOPE ~ 2, LARGER HOSTS HAVE DISPROPORTIONATELY LARGER PARASITES HOSTS LIVE LONGER, SO PARASITES CAN GROW BIGGER AND BE MORE FECUND?)





#### Hatton, Dobson, et al, submitted.





**A**. Mammal specific metabolism across different activity states. Maximum (k = -0.07) and minimum torpor (k = -0.04) are compared with basal rates (grey points; k = -0.28), and three types of experimental cell cultures: skeletal, hepatocyte and fibroblast, where the sizes of the latter two are shown in C. Data are not temperature corrected for reasons outlined in Methods, but would shift torpor closer to basal rates.

**B.** Mammal specific growth across different life stages. Ontogenetic growth (k = -0.28) and prenatal growth (k = -0.29) are compared with reproductive growth (grey points; k = -0.28).

**C.** Mammal average cell sizes. Cell volume was converted to mass assuming 1 gram= $10^{12} \mu m^3$ . Sperm and egg cells are excluded and are typically the smallest and largest cells, respectively. Grey dashed lines are regressions for other specific cell types not listed. In total, only six of 28 cell types show significant positive relations: adipocyte, epidermis, alveolar macrophage, and three types of neurons, all with shallow slopes of k < 0.2.

- Do the dynamics of the Immune Systems Scale with Size/Mass of its Constituents. Can we use this to make next generation models of immune systems (as food-webs)
- Do incubation periods and durations and infectivity change with host age? Do these also change as virus and bacteria 'age'
- How can we tease apart background rates of infection from age-dependent changes in susceptibility and transmission efficiency

## EMERGING QUESTIONS